

### 3.0 Multiply Radicals

Math 20-2

Radicals

number x number

Skill Review: multiply polynomials: VAR x VAR

$$3(2x) = 6x$$

$$5x(4x + 3) = 20x^2 + 15x$$

$$(3x - 4)(2x - 5) = 6x^2 - 15x - 8x + 20$$

$$= 6x^2 - 23x + 20$$

**Objective: Multiply and Simplify Radical Expressions.**

1. Monomial Multiplication (whole by whole & radical by radical). Multiply the following radicals and simplify if possible.

a.  $\sqrt{5} \times \sqrt{6}$

$$= \sqrt{30}$$

b.  $\sqrt{6} \times \sqrt{7}$

$$= \sqrt{42}$$

..multiply..

c.  $3\sqrt{6} \times \sqrt{15}$

$$= 3\sqrt{90}$$

$$= 3\sqrt{9}\sqrt{10}$$

$$= 3(3)\sqrt{10}$$

$$= 9\sqrt{10}$$

d.  $3\sqrt{5} \times 4\sqrt{8}$

$$= 12\sqrt{40}$$

$$= 12\sqrt{4}\sqrt{10}$$

$$= 12(2)\sqrt{10}$$

$$= 24\sqrt{10}$$

..simplify..

e.  $\sqrt{18} \times \sqrt{15}$

$$= \sqrt{9}\sqrt{2} \times \sqrt{15}$$

$$= 3\sqrt{2} \times \sqrt{15}$$

$$= 3\sqrt{30}$$

f.  $\sqrt{20} \times \sqrt{12}$

multiply

$$\sqrt{20} \times \sqrt{12}$$

$$= \sqrt{240}$$

$$= \sqrt{16}\sqrt{15}$$

$$= 4\sqrt{15}$$

vs simplify

$$= \sqrt{4}\sqrt{5} \times \sqrt{4}\sqrt{3}$$

$$= 2\sqrt{5} \times 2\sqrt{3}$$

$$= 4\sqrt{15}$$

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2. **Distributive Property.** Multiply and simplify wherever possible.

$$\begin{aligned}
 & a. \quad 3(5\sqrt{2}-7) \\
 & = 15\sqrt{2} - 21
 \end{aligned}$$

$$\begin{aligned}
 & b. \quad \sqrt{2}(3\sqrt{6}+\sqrt{10}) \\
 & = 3\sqrt{12} + \sqrt{20} \\
 & = 3\sqrt{4\sqrt{3}} + \sqrt{4\sqrt{5}} \\
 & = 3(2)\sqrt{3} + 2\sqrt{5} \\
 & = 6\sqrt{3} + 2\sqrt{5}
 \end{aligned}$$

$$\begin{aligned}
 & c. \quad (\sqrt{2}+\sqrt{5})(3\sqrt{6}-2\sqrt{10}) \\
 & = 3\sqrt{12} - 2\sqrt{20} + 3\sqrt{30} - 2\sqrt{50} \\
 & = 3\sqrt{4\sqrt{3}} - 2\sqrt{4\sqrt{5}} + 3\sqrt{30} - 2\sqrt{25\sqrt{2}} \\
 & = 3(2)\sqrt{3} - 2(2)\sqrt{5} + 3\sqrt{30} - 2(5)\sqrt{2} \\
 & = 6\sqrt{3} - 4\sqrt{5} + 3\sqrt{30} - 10\sqrt{2}
 \end{aligned}$$

$$\begin{aligned}
 & d. \quad (5\sqrt{2}-2\sqrt{6})(5\sqrt{2}-2\sqrt{6}) \\
 & = 25\sqrt{4} - 10\sqrt{12} - 10\sqrt{12} + 4\sqrt{36} \\
 & = 25(2) - 20\sqrt{4\sqrt{3}} + 4(6) \\
 & = 50 - 20\sqrt{4\sqrt{3}} + 24 \\
 & = 74 - 20(2)\sqrt{3} \\
 & = 74 - 40\sqrt{3}
 \end{aligned}$$

$$\begin{aligned}
 & e. \quad (\sqrt{5}+\sqrt{3})(\sqrt{5}-\sqrt{3}) \\
 & = \sqrt{25} - \underbrace{\sqrt{15} + \sqrt{15}}_{\text{zero}} - \sqrt{9} \\
 & = \sqrt{25} - \sqrt{9} \\
 & = 5 - 3 \\
 & = 2
 \end{aligned}$$

$$\begin{aligned}
 & f. \quad (2+7\sqrt{5})(2+\sqrt{5}) \\
 & = 4 + 2\sqrt{5} + 14\sqrt{5} + 7\sqrt{25} \\
 & = 4 + 16\sqrt{5} + 7(5) \\
 & = 4 + 16\sqrt{5} + 35 \\
 & = 39 + 16\sqrt{5}
 \end{aligned}$$