

Trigonometry Quiz - 2017

1. Solve:

- a) Solve for side indicated, rounded to one decimal place.

$$\text{i. } \frac{5.4}{\sin 70} = \frac{x}{\sin 80}$$

$$x = 5.4(\sin 80) \div \sin 70 = 5.659$$

$$x = 5.7$$

$$\text{ii. } x^2 = 7.5^2 + 4.2^2 - 2(7.5)(4.2)\cos 72$$

$$x^2 = 54.42$$

$$x = 7.4$$

[4]

- b) Find the measure of A to the nearest degree.

$$\text{i. } \frac{15}{\sin A} = \frac{12}{\sin 50} \quad \sin A = \frac{15(\sin 50)}{12} = 0.9576$$

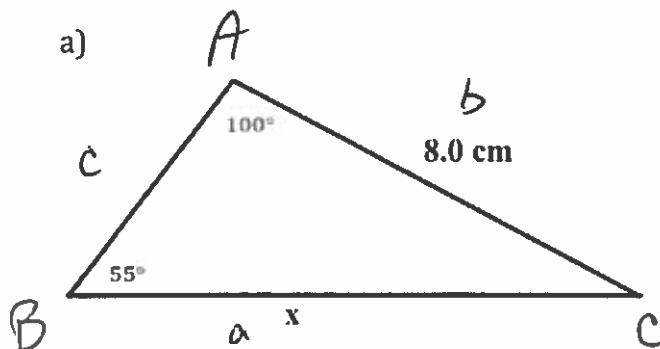
$$A = \sin^{-1}(0.9576) = 73^\circ$$

$$\text{ii. } \cos A = \frac{6.0^2 + 9.0^2 - 8.0^2}{2(6.0)(9.0)}$$

$$\cos A = \frac{53}{108} \quad \cos^{-1}\left(\frac{53}{108}\right)$$

$$A = 61^\circ$$

2. Label the triangles using A, B, and C for the angles and using a, b and c for the sides.
 Find the length of the side indicated, round to one decimal place.



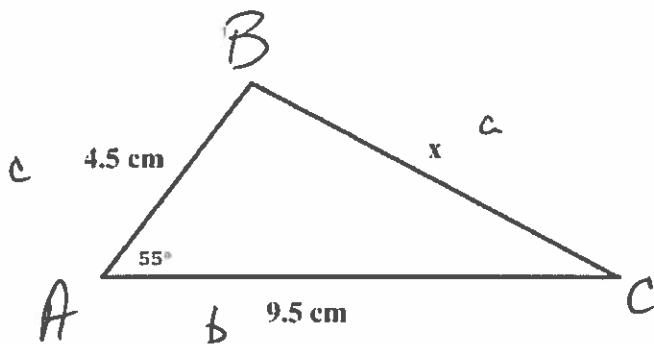
$$\frac{x}{\sin 100^\circ} = \frac{8.0}{\sin 55^\circ}$$

$$x = \frac{8.0(\sin 100^\circ)}{\sin 55^\circ}$$

$$x = 9.6$$

[4]

b)



$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$x^2 = 9.5^2 + 4.5^2 - 2(9.5)(4.5) \cos 55^\circ$$

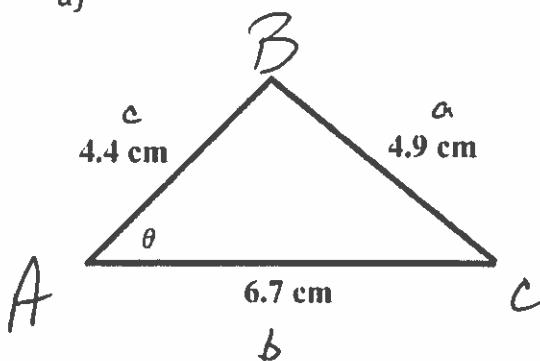
$$x^2 = 61.46$$

$$x = 7.8$$

3. Label the triangles using A, B, and C for the angles and using a, b and c for the sides.

Find the measure of the angle indicated, round to a whole number.

a)



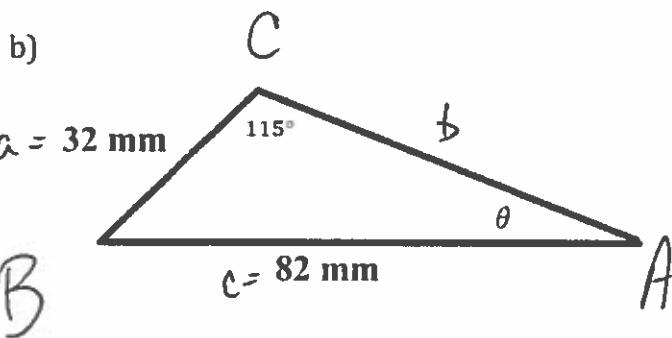
$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

$$\cos A = \frac{6.7^2 + 4.4^2 - 4.9^2}{2(6.7)(4.4)}$$

$$\cos A = \frac{40.24}{58.96}$$

$$A = 47^\circ$$

[4]



$$\frac{32}{\sin \theta} = \frac{82}{\sin 115^\circ}$$

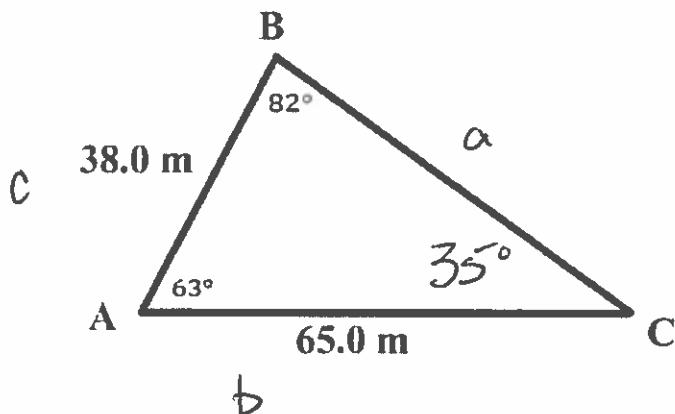
$$\sin \theta = \frac{32 \sin 115^\circ}{82} = 0.3537$$

$$\theta = \sin^{-1}(0.3537)$$

$$\theta = 21^\circ$$

4. ~~x~~ Solve the triangle.

[3]



$$C = 180 - 63 - 82$$

$$C = 35^\circ$$

$$\frac{a}{\sin 63} = \frac{65}{\sin 82} \quad \boxed{\text{OR}} \quad a^2 = 65^2 + 38^2 - 2(65)(38) \cos 63^\circ$$

$$a = \frac{65(\sin 63)}{\sin 82}$$

$$a^2 = 3426.3$$

$$a = 58.5$$

$$a = 58.5$$

OR

$$\frac{a}{\sin 63} = \frac{38}{\sin 35}$$

$$a = \frac{38(\sin 63)}{\sin 35}$$

$$a = 59.0$$